



COMPLEMENT AND μ -COMPLEMENT OF INTUITIONISTIC FUZZY SOFT GRAPH

Y. Preethi Ceon

Assistant Professor, KG College of Arts and Science, Coimbatore-641035, Tamil Nadu

Abstract

In this paper, the basic definitions of intuitionistic fuzzy soft graph, strong and complete intuitionistic fuzzy soft graph are introduced. The notions of complement and μ -complement of intuitionistic fuzzy soft graph are introduced and also some of their properties are investigated.

Keywords - Intuitionistic fuzzy soft graph, Strong IFSG, Complete IFSG, μ -Complement IFSG.

1.Introduction

In 1999, Soft set theory is applied to smooth of functions, game theory, operations research, probability and measurement theory by Molodstov[1,2]. The notions of soft trees, soft cycles, soft bridges, soft ctnodes and describe a various methods of construction of soft trees are discussed by Akram and Nawaz [3].

The concept of soft set theory to solve imprecise problems in the field of engineering, social science, economics, medical science and environment are discussed Molodstov [4] in 1999. Molodstov [4,5] applied soft set theory to several directions. In recent times, a number of researchers were more active doing research on soft set. Anas AI-Masarwah, Majdoleen Abu Qamar [6] discussed about the complement of fuzzy soft graph and isolated fuzzy soft graph. A.M.Shyla and T.M.Mathew Varkey [7] discussed strong and complete intuitionistic fuzzy soft graph.

In this paper the author discussed about the μ -complements of intuitionistic fuzzy soft graph.

2.PRELIMINARIES

Definition 2.1

A pair (F,A) is called fuzzy soft set over U , where F is a mapping given by $F :A \rightarrow F^U$; F^U denotes the collection of all fuzzy subsets of U ; $A \subseteq P$.

Definition 2.2

Let $G= (V,E)$ be a simple graph, $V= \{v_1, v_2 \dots v_n\}$ (non-empty set), $E \subseteq V \times V$, P (parameter set) and $A \subseteq P$.Also let

1. μ_i is a function defined on V by

$$\mu_i : A \rightarrow F^U(V) \quad (F^U(V) \text{ denotes collection of all fuzzy subsets in } V)$$

$$a \mapsto \mu_i(a) = \mu_{ia} \text{ (say) , } a \in A \text{ and } \mu_{ia} : V \rightarrow [0,1], v_i \mapsto \mu_{ia}(v_i)$$

(A, μ_i) fuzzy soft vertex and

2. μ_{ij} is a function defined on E by

$\mu_{ij} : A \rightarrow F^U(V \times V)$ ($F^U(V \times V)$ denotes collection of all fuzzy subsets in E)

$a \mapsto \mu_{ij}(a) = \mu_{ija}$ (say), $a \in A$ and $\mu_{ija} : V \times V \rightarrow [0,1]$, $(v_i, v_j) \mapsto \mu_{ija}(v_i, v_j)$

(A, μ_{ij}) fuzzy soft edge.

A pair $((A, \mu_i), (A, \mu_{ij}))$ is called a fuzzy soft graph. If $\mu_{ija}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) \forall$

$(v_i, v_j) \in E$ and $a \in A$

Definition 2.3

A pair (\tilde{F}, A) is called intuitionistic fuzzy soft set over U, where \tilde{F} is a mapping given by the $\tilde{F} : A \rightarrow IF^U$; IF^U denotes the collection of all intuitionistic fuzzy subsets of U; $A \subseteq P$.

Definition 2.4

Let $G = (V, E)$ be a simple graph, $V = \{v_1, v_2 \dots v_n\}$ (non-empty set), $E \subseteq V \times V$, P (parameter set) and $A \subseteq P$. Also let

1. μ_i is a membership function defined on V by

$\mu_i : A \rightarrow IF^U(V)$ ($IF^U(V)$ denotes collection of all intuitionistic fuzzy subsets in V)

$a \mapsto \mu_i(a) = \mu_{ia}$ (say), $a \in A$ and $\mu_{ia} : V \rightarrow [0,1]$, $v_i \mapsto \mu_{ia}(v_i)$

(A, μ_i) Intuitionistic fuzzy soft vertex of membership function and

ν_i is a membership function defined on V by

$\nu_i : A \rightarrow IF^U(V)$ ($IF^U(V)$ denotes collection of all intuitionistic fuzzy subsets in V)

$a \mapsto \nu_i(a) = \nu_{ia}$ (say), $a \in A$ and $\nu_{ia} : V \rightarrow [0,1]$, $v_i \mapsto \nu_{ia}(v_i)$

(A, ν_i) Intuitionistic fuzzy soft vertex of membership function such that

$0 \leq \mu_{ia}(v_i) + \nu_{ia}(v_i) \leq 1$, for every $v_i \in V$, $i=1,2,\dots,n$ and $a \in A$.

2. μ_{ij} is a membership function defined on E by

$\mu_{ij} : A \rightarrow IF^U(V \times V)$ ($IF^U(V \times V)$ denotes collection of all intuitionistic fuzzy subsets in E)

$a \mapsto \mu_{ij}(a) = \mu_{ija}$ (say), $a \in A$ and $\mu_{ija} : V \times V \rightarrow [0,1]$, $(v_i, v_j) \mapsto \mu_{ija}(v_i, v_j)$

ν_{ij} is a non-membership function defined on E by

$\nu_{ij} : A \rightarrow IF^U(V \times V)$ ($IF^U(V \times V)$ denotes collection of all intuitionistic fuzzy subsets in E)

$a \mapsto \nu_{ij}(a) = \nu_{ija}$ (say), $a \in A$ and $\nu_{ija} : V \times V \rightarrow [0,1]$, $(v_i, v_j) \mapsto \nu_{ija}(v_i, v_j)$

where $((A, \mu_{ij}), (A, \nu_{ij}))$ are intuitionistic fuzzy soft edge of membership and non-membership function satisfying

$$\mu_{ija}(v_i, v_j) \leq \min\{\mu_{ia}(v_i), \mu_{ia}(v_j)\} \quad \nu_{ija}(v_i, v_j) \leq \max\{\nu_{ia}(v_i), \nu_{ia}(v_j)\} \text{ and}$$

$$0 \leq \mu_{ija}(v_i, v_j) + \nu_{ija}(v_i, v_j) \leq 1,$$

$$0 \leq \mu_{ija}(v_i, v_j), \nu_{ija}(v_i, v_j) \leq 1, \text{ for every } (v_i, v_j) \in E, i, j = 1, 2, \dots, n \text{ and } a \in A$$

Then $G = (V, E, (A, \mu_1), (A, \gamma_1), (A, \mu_2), (A, \gamma_2))$ is said to be Intuitionistic fuzzy soft graph (IFSG) and this IFSG is denoted by $G_{A,V,E}$.

Definition 2.5

Let $G_{A,V,E}$ be an intuitionistic fuzzy soft graph. It is said to be strong intuitionistic fuzzy soft graph if $\mu_{ija}(v_i, v_j) = \min\{\mu_{ia}(v_i), \mu_{ia}(v_j)\}$ and $\nu_{ija}(v_i, v_j) = \max\{\nu_{ia}(v_i), \nu_{ia}(v_j)\}$ forevery $(v_i, v_j) \in E$, and $a \in A$

Definition 2.6

Let $G_{A,V,E}$ be an intuitionistic fuzzy soft graph. It is said to be complete intuitionistic fuzzy soft graph if $\mu_{ija}(v_i, v_j) = \min\{\mu_{ia}(v_i), \mu_{ia}(v_j)\}$ and $\nu_{ija}(v_i, v_j) = \max\{\nu_{ia}(v_i), \nu_{ia}(v_j)\}$ forevery $(v_i, v_j) \in V$, and $a \in A$

Definition 2.7

Let $G_{A,V,E}$ be an intuitionistic fuzzy soft graph. The complement of a $G_{A,V,E}$ is defined as $\overline{G_{A,V,E}} = (V, E, (A, \mu_i), (A, \nu_i), (\overline{A, \mu_{ij}}), (\overline{A, \nu_{ij}}))$ where

$$\overline{\mu_{ija}(v_i, v_j)} = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) - \mu_{ija}(v_i, v_j)$$

$$\overline{\nu_{ija}(v_i, v_j)} = \nu_{ia}(v_i) \vee \nu_{ia}(v_j) - \nu_{ija}(v_i, v_j) \text{ for all } v_i, v_j \in V, a \in A.$$

Definition 2.8

If $G_{A,V,E}$ be an intuitionistic fuzzy soft graph. $G_{A,V,E}^\mu$ is a μ - complement of a $G_{A,V,E}$ is defined as $G_{A,V,E}^\mu = (V, E, (A, \mu_i), (A, \nu_i), (A, \mu_{ij})^\mu, (A, \nu_{ij})^\mu)$ where

$$\mu_{ija}^{\mu}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) - \mu_{ija}(v_i, v_j)$$

$$v_{ija}^{\mu}(v_i, v_j) = v_{ia}(v_i) \vee v_{ia}(v_j) - v_{ija}(v_i, v_j) \text{ for all } v_i, v_j \in V, a \in A.$$

3. Main results of IFSG

Theorem 3.1

If $G_{A,V,E}$ be an intuitionistic fuzzy soft graph. Then $G_{A,V,E}$ is an isolated intuitionistic fuzzy soft graph if and only if $\overline{G_{A,V,E}}$ is a strong intuitionistic fuzzy soft graph.

Proof

Given $G_{A,V,E}$ be an intuitionistic fuzzy soft graph. The complement of a $G_{A,V,E}$ is defined by $\overline{G_{A,V,E}}$

$$\overline{\mu_{ija}}(v_i, v_j) = 0 \quad \overline{v_{ija}}(v_i, v_j) = 0 \text{ for all } v_i, v_j \in V \times V, a \in A.$$

Since

$$\overline{\mu_{ija}}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) - \mu_{ija}(v_i, v_j) \text{ for all } v_i, v_j \in V \times V, a \in A.$$

$$\overline{\mu_{ija}}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) \text{ for all } v_i, v_j \in V \times V, a \in A.$$

$$\overline{v_{ija}}(v_i, v_j) = v_{ia}(v_i) \vee v_{ia}(v_j) - v_{ija}(v_i, v_j) \text{ for all } v_i, v_j \in V \times V, a \in A.$$

$$\overline{v_{ija}}(v_i, v_j) = v_{ia}(v_i) \vee v_{ia}(v_j) \text{ for all } v_i, v_j \in V \times V, a \in A.$$

$$\overline{\mu_{ija}}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j), \overline{v_{ija}}(v_i, v_j) = v_{ia}(v_i) \vee v_{ia}(v_j) \text{ for all } v_i, v_j \in V \times V, a \in A.$$

Hence $\overline{G_{A,V,E}}$ is a strong intuitionistic fuzzy soft graph.

Conversely,

Given $\overline{G_{A,V,E}}$ is a strong intuitionistic fuzzy soft graph.

$$\overline{\mu_{ija}}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j), \overline{v_{ija}}(v_i, v_j) = v_{ia}(v_i) \vee v_{ia}(v_j) \text{ for all } v_i, v_j \in V \times V, a \in A.$$

Since

$$\mu_{ija}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) - \overline{\mu_{ija}}(v_i, v_j) \text{ for all } v_i, v_j \in V \times V, a \in A.$$

$$= \overline{\mu_{ija}}(v_i, v_j) - \overline{\mu_{ija}}(v_i, v_j) \text{ for all } v_i, v_j \in V \times V, a \in A.$$

$$\mu_{ija}(v_i, v_j) = 0 \text{ for all } v_i, v_j \in V \times V, a \in A.$$

$$\begin{aligned} \nu_{ija}(v_i, v_j) &= \nu_{ia}(v_i) \vee \nu_{ia}(v_j) - \overline{\nu_{ija}(v_i, v_j)} \text{ for all } v_i, v_j \in V \times V, a \in A. \\ &= \overline{\nu_{ija}(v_i, v_j)} - \overline{\nu_{ija}(v_i, v_j)} \text{ for all } v_i, v_j \in V \times V, a \in A. \end{aligned}$$

$$\nu_{ija}(v_i, v_j) = 0 \text{ for all } v_i, v_j \in V \times V, a \in A.$$

$$\mu_{ija}(v_i, v_j) = 0 \text{ and } \nu_{ija}(v_i, v_j) = 0 \text{ for all } v_i, v_j \in V \times V, a \in A.$$

Hence, $G_{A,V,E}$ is an isolated intuitionistic fuzzy soft graph.

Theorem 3.2

If $G_{A,V,E} = (V, E, (A, \mu_i), (A, \nu_i), (A, \mu_{ij}), (A, \nu_{ij}))$ be an intuitionistic fuzzy soft graph. Then $G_{A,V,E}^\mu$ is an isolated intuitionistic fuzzy soft graph if and only if $G_{A,V,E}$ is a strong intuitionistic fuzzy soft graph.

Proof

Given $G_{A,V,E} = (V, E, (A, \mu_i), (A, \nu_i), (A, \mu_{ij}), (A, \nu_{ij}))$ be an intuitionistic fuzzy soft graph. The μ -complement of $G_{A,V,E}$ is denoted by $G_{A,V,E}^\mu$. Let $G_{A,V,E} = (V, E, (A, \mu_i), (A, \nu_i), (A, \mu_{ij}), (A, \nu_{ij}))$ be an strong intuitionistic fuzzy soft graph. If

$\mu_{ija}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j)$ and $\nu_{ija}(v_i, v_j) = \nu_{ia}(v_i) \vee \nu_{ia}(v_j) \forall (v_i, v_j) \in E$ and $a \in A$ otherwise

$$\mu_{ija}(v_i, v_j) = 0 \text{ and } \nu_{ija}(v_i, v_j) = 0$$

By the definition of μ -complement and from equations (1) and (2)

$$\mu_{ija}^\mu(v_i, v_j) = 0 \text{ and } \nu_{ija}^\mu(v_i, v_j) = 0 \forall (v_i, v_j) \in E \text{ and } a \in A$$

Hence, $G_{A,V,E}^\mu$ is an isolated intuitionistic fuzzy soft graph.

Conversely,

Assume $G_{A,V,E}^\mu$ is an isolated intuitionistic fuzzy soft graph.

For a membership function

$$\Rightarrow \mu_{ija}^\mu(v_i, v_j) = 0 \forall (v_i, v_j) \in E \text{ and } a \in A$$

$$\Rightarrow \mu_{ija}^\mu(v_i, v_j) = 0 \forall (v_i, v_j) \in \mu^* \text{ and } (v_i, v_j) \notin \mu^* \text{ } a \in A$$

From the definition if $(v_i, v_j) \in \mu^*$

$$\mu_{ija}^\mu(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) - \mu_{ija}(v_i, v_j)$$

Since

$$\mu_{ija}^{\mu}(v_i, v_j) = 0$$

$$0 = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) - \mu_{ija}(v_i, v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

$$\mu_{ija}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

For a non-membership function

$$\Rightarrow \quad \nu_{ija}^{\mu}(v_i, v_j) = 0 \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

$$\Rightarrow \quad \nu_{ija}^{\mu}(v_i, v_j) = 0 \quad \forall (v_i, v_j) \in \nu^* \text{ and } (v_i, v_j) \notin \nu^* \quad a \in A$$

From the definition if $(v_i, v_j) \in \nu^*$

$$\nu_{ija}^{\mu}(v_i, v_j) = \nu_{ia}(v_i) \vee \nu_{ia}(v_j) - \nu_{ija}(v_i, v_j)$$

Since

$$\nu_{ija}^{\mu}(v_i, v_j) = 0$$

$$\Rightarrow \quad 0 = \nu_{ia}(v_i) \vee \nu_{ia}(v_j) - \nu_{ija}(v_i, v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

$$\Rightarrow \quad \nu_{ija}(v_i, v_j) = \nu_{ia}(v_i) \vee \nu_{ia}(v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

Therefore,

$$\mu_{ija}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) \text{ and } \nu_{ija}(v_i, v_j) = \nu_{ia}(v_i) \vee \nu_{ia}(v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

Hence,

$G_{A,V,E} = (V, E, (A, \mu_i), (A, \nu_i), (A, \mu_{ij}), (A, \nu_{ij}))$ be an strong intuitionistic fuzzy soft graph.

Theorem 3.3

If $G_{A,V,E} = (V, E, (A, \mu_i), (A, \nu_i), (A, \mu_{ij}), (A, \nu_{ij}))$ be an intuitionistic fuzzy soft graph. Then $G_{A,V,E}^{\mu}$ is an isolated intuitionistic fuzzy soft graph if and only if $G_{A,V,E}$ is a complete intuitionistic fuzzy soft graph.

Proof

Given $G_{A,V,E} = (V, E, (A, \mu_i), (A, \nu_i), (A, \mu_{ij}), (A, \nu_{ij}))$ be an intuitionistic fuzzy soft graph. The μ -complement of $G_{A,V,E}$ is denoted by $G_{A,V,E}^{\mu}$. Let $G_{A,V,E} = (V, E, (A, \mu_i), (A, \nu_i), (A, \mu_{ij}), (A, \nu_{ij}))$ be an strong intuitionistic fuzzy soft graph. If

$\mu_{ija}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j)$ and $\nu_{ija}(v_i, v_j) = \nu_{ia}(v_i) \vee \nu_{ia}(v_j) \quad \forall (v_i, v_j) \in E$ and $a \in A$
 otherwise

$$\mu_{ija}(v_i, v_j) = 0 \text{ and } \nu_{ija}(v_i, v_j) = 0$$

By the definition of μ -complement and from equations (1) and (2)

$$\mu_{ija}^{\mu}(v_i, v_j) = 0 \text{ and } \nu_{ija}^{\mu}(v_i, v_j) = 0 \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

Hence, $G_{A,V,E}^{\mu}$ is an isolated intuitionistic fuzzy soft graph.

Conversely,

Assume $G_{A,V,E}^{\mu}$ is an isolated intuitionistic fuzzy soft graph.

For a membership function

$$\Rightarrow \mu_{ija}^{\mu}(v_i, v_j) = 0 \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

$$\Rightarrow \mu_{ija}^{\mu}(v_i, v_j) = 0 \quad \forall (v_i, v_j) \in \mu^* \text{ and } (v_i, v_j) \notin \mu^* \quad a \in A$$

From the definition if $(v_i, v_j) \in \mu^*$

$$\mu_{ija}^{\mu}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) - \mu_{ija}(v_i, v_j)$$

Since

$$\mu_{ija}^{\mu}(v_i, v_j) = 0$$

$$0 = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) - \mu_{ija}(v_i, v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

$$\mu_{ija}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

For a non-membership function

$$\Rightarrow \nu_{ija}^{\mu}(v_i, v_j) = 0 \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

$$\Rightarrow \nu_{ija}^{\mu}(v_i, v_j) = 0 \quad \forall (v_i, v_j) \in \nu^* \text{ and } (v_i, v_j) \notin \nu^* \quad a \in A$$

From the definition if $(v_i, v_j) \in \nu^*$

$$\nu_{ija}^{\mu}(v_i, v_j) = \nu_{ia}(v_i) \vee \nu_{ia}(v_j) - \nu_{ija}(v_i, v_j)$$

Since

$$v_{ija}^\mu (v_i, v_j) = 0$$

$$\Rightarrow 0 = v_{ia}(v_i) \vee v_{ia}(v_j) - v_{ija}(v_i, v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

$$\Rightarrow v_{ija}(v_i, v_j) = v_{ia}(v_i) \vee v_{ia}(v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

Therefore,

$$\mu_{ija}(v_i, v_j) = \mu_{ia}(v_i) \wedge \mu_{ia}(v_j) \text{ and } v_{ija}(v_i, v_j) = v_{ia}(v_i) \vee v_{ia}(v_j) \quad \forall (v_i, v_j) \in E \text{ and } a \in A$$

Hence,

$G_{A,V,E} = (V, E, (A, \mu_i), (A, v_i), (A, \mu_{ij}), (A, v_{ij}))$ be an complete intuitionistic fuzzy soft graph.

Conclusion

In this paper, the definitions of intuitionistic fuzzy soft graphs, complete and strong intuitionistic fuzzy soft graphs are discussed. Also studied about their μ -complement. In future, the author proposed to continue this result in interval-valued intuitionistic fuzzy soft graphs and self-complementary intuitionistic fuzzy soft graphs.

REFERENCES

1. M.Akram, S.Nawaz, On fuzzy soft graphs, *Italian Journal of Pure and Applied Mathematics* 34(2015) 497-514.
2. M.Akram, S.Nawaz, Operations on soft graphs, *Fuzzy Information and Engineering* 7(4)(2015) 423-449.
3. M.Akram, F.Zafar, On soft trees, *Buletinul Academiei de Stiinte a Republicii Moldova* 2(78)(2015) 82-95.
4. D.A.Moldtsov, Soft set theory-first results, *Computer and Mathematics With Applications* 37(1999) 19-31.
5. D.A.Moldtsov, the theory of soft sets(in Russian), *URSS Publishers*, Moscow,2004.
6. Anas Al-Masarwah, Majdoleen Abu Qamar, Some new concepts of fuzzy soft graphs, *Fuzzy Information and Engineering*(2016)8 427-438.
7. A.M.Shyla and T.M.Mathew Varkey, Intuitionistic Fuzzy soft graph, *International Journal of Fuzzy Mathematical Archive* vol-11,No.2,2016,63-77.
8. P.K.Maji, R.Biswas and A.R.Roy, Intuitionistic fuzzy soft sets, *The Journal of Fuzzy Mathematics*, 9(3) (2001) 677-692.
9. P.Majumdar and S.K.Samanta, Generalized fuzzy soft sets, *Computers and Mathematics with Applications*, 59 (2010) 1425-1432.
10. D.A.Molodtsov, Soft set theory- first results, *Compt. Math. Appl.*, 37 (1999) 19-31. 14. D.A.Molodtsov, The description of a dependance with the help of soft sets, *J. Compt. Sys. Sc. Int.*, 40 (6) (2001) 977-984.
11. D.A.Molodtsov, *The Theory of Soft Sets* (in Russian), URSS Publishers, Moscow, 2004.
12. D.A.Molodtsov, V.Yu.Leonov and D.V.Kovkov, soft set technique and its application, *Nechetkie Sistemi I Myakie Vychisleniya*, 1(1) (2006) 8-39.
13. T.J.Neog and D.K.Sut, On fuzzy soft complement and related properties, *International Journal of Energy, Inforation and Communication*.
14. R.K.Thumbakara and B.George, Soft graph, *Gen. Math. Notes*, 21(2) (2014) 75-86.